

Programming Abstractions

Lecture 32: Streams 2

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Streams in Racket

These are already built-in so we don't need to write them

- ▶ `(require racket/stream)`
- ▶ `(stream exp ...)` ; Works like `(list exp ...)`
- ▶ `(stream? v)`
- ▶ `(stream-cons head tail)`
- ▶ `(stream-first s)`
- ▶ `(stream-rest s)`
- ▶ `(stream-empty? s)`
- ▶ `empty-stream`
- ▶ `(stream-ref s idx)`

And several others

Constructing an infinite-length stream

Simplest infinite-length stream: A stream of all zeros

```
(define all-zeros  
  (stream-cons 0 all-zeros))
```

Note that we couldn't do this with a list

```
(define all-zeros-lst  
  (cons 0 all-zeros-lst))
```

**Error: all-zeros-lst: undefined;
cannot reference an identifier before its definition**

Why does

```
(define all-zeros  
  (stream-cons 0 all-zeros))  
work when the list-version does not?
```

- A. Streams are magic
- B. Streams are lazy so the stream-cons doesn't run until all-zeros is accessed for the first time
- C. Streams are lazy so although the stream is constructed by stream-cons, its "first" and "rest" part aren't evaluated until forced by stream-first and stream-rest
- D. Racket treats streams specially so it knows this construction is okay

`(stream-length s)` is a standard Racket stream function that returns the length of the stream

What is the result of this code?

```
(define all-zeros
  (stream-cons 0 all-zeros))
(stream-length all-zeros)
```

- A. 0
- B. `+inf.0` (which is how Racket spells positive infinity)
- C. `+nan.0` (which is how Racket spells Not a Number (NaN))
- D. Infinite loop
- E. Error

Constructing an infinite-length stream

Write a procedure which

- returns a stream constructed via `stream-cons`
- where the tail of the stream is a `recursive call` to the procedure

Call the procedure with the initial argument

```
(define (integers-from n)
  (stream-cons n (integers-from (add1 n))))
```

```
(define positive-integers (integers-from 0))
```

Primes as a stream

```
(define (prime? n) ...) ; Returns #t if n is prime
```

```
(define (next-prime n)
  (cond [(prime? n) (stream-cons n (next-prime (+ n 2)))]
        [else (next-prime (+ n 2))]))
```

```
(define (primes)
  (stream-cons 2 (next-prime 3)))
```

Fibonacci numbers as a stream

Recall the Fibonacci numbers are defined by $f_0 = 0$, $f_1 = 1$ and $f_n = f_{n-1} + f_{n-2}$

```
(define (next-fib m n)
  (stream-cons m (next-fib n (+ m n))))
```

```
(define fibs (next-fib 0 1))
```


Fibonacci numbers as a stream: take 2

$$f_0 = 0, f_1 = 1 \text{ and } f_n = f_{n-1} + f_{n-2}$$

We can build our Fibonacci sequence directly from that definition (this is silly)

```
(define fibs
  (stream-cons
    0
    (stream-cons
      1
      (stream-add fibs (stream-rest fibs)))))
```

Write some infinite-length streams

- ▶ `(constant-stream x)`

Returns a stream containing an infinite number of x

```
(stream->list (stream-take (constant-stream 'ha) 10))
```

```
=> '(ha ha ha ha ha ha ha ha ha ha)
```

- ▶ `(define abc ...)`

Define an infinite-length stream (not a function) consisting of 'A, 'B, 'C repeating in order. [Hint: `(stream* ...)` makes this short]

```
(stream->list (stream-take abc 12))
```

```
=> '(A B C A B C A B C A B C)
```

- ▶ `(stream-cycle s)`

Returns an infinite-length stream consisting of the elements of s repeating in order. E.g., the abc stream could be rewritten as

```
(stream-cycle (stream 'A 'B 'C))
```

Write some stream procedures

▶ `(stream-double s)`

Returns a stream containing each element of `s` twice

`(stream-double (stream 1 2 3)) => (stream 1 1 2 2 3 3)`

▶ `(stream-interleave s t)`

Returns a stream that interleaves elements of `s` and `t`

`(stream-interleave (stream 1 2 3) '(a b c d))`
`=> (stream 1 'a 2 'b 3 'c 'd)`

Write more stream procedures

Write the following procedures that act like their list counterparts, but operate lazily on streams; in particular, do not convert them to lists!

- ▶ `(stream-take s num)`
Returns a stream containing the first `num` elements of `s`, make sure this is lazy
- ▶ `(stream-drop s num)`
Returns a stream containing all of the elements of `s` in order *except* for the first `num`
- ▶ `(stream-filter f s)`
Returns a stream containing the elements `x` of `s` for which `(f x)` returns true

Multi-argument stream-map

```
(stream-map f s ...)
```

Racket has stream-map built-in but unlike its list counterparts, it only takes a single stream

Generalize it to take any number of streams where the length of the returned string is the minimum length of any of the stream arguments (i.e., return empty-stream if any of the streams becomes empty); you'll want to use ormap, map and apply

```
▸ (define (stream-map f . ss) ...)
```